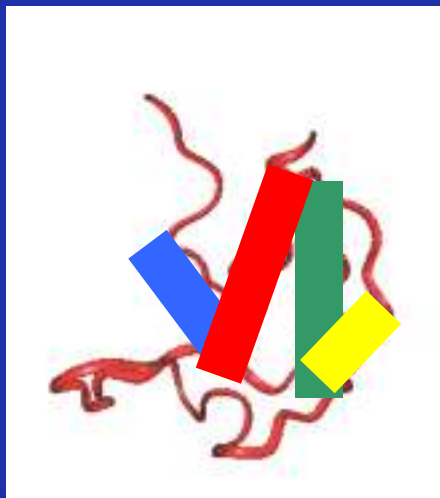
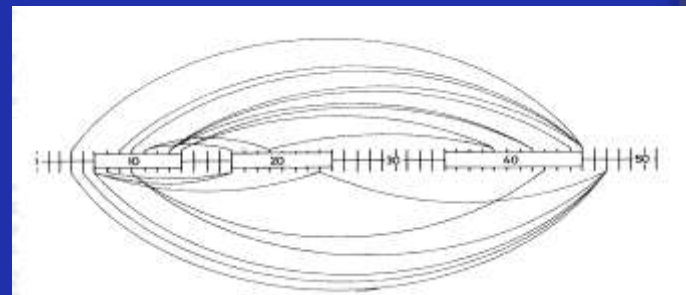
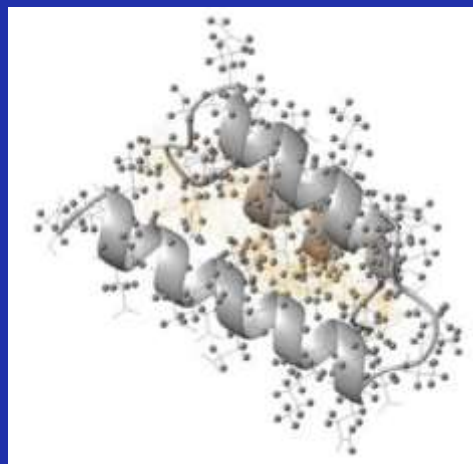


# 蛋白质核磁共振结构解析示意图

Unfolded



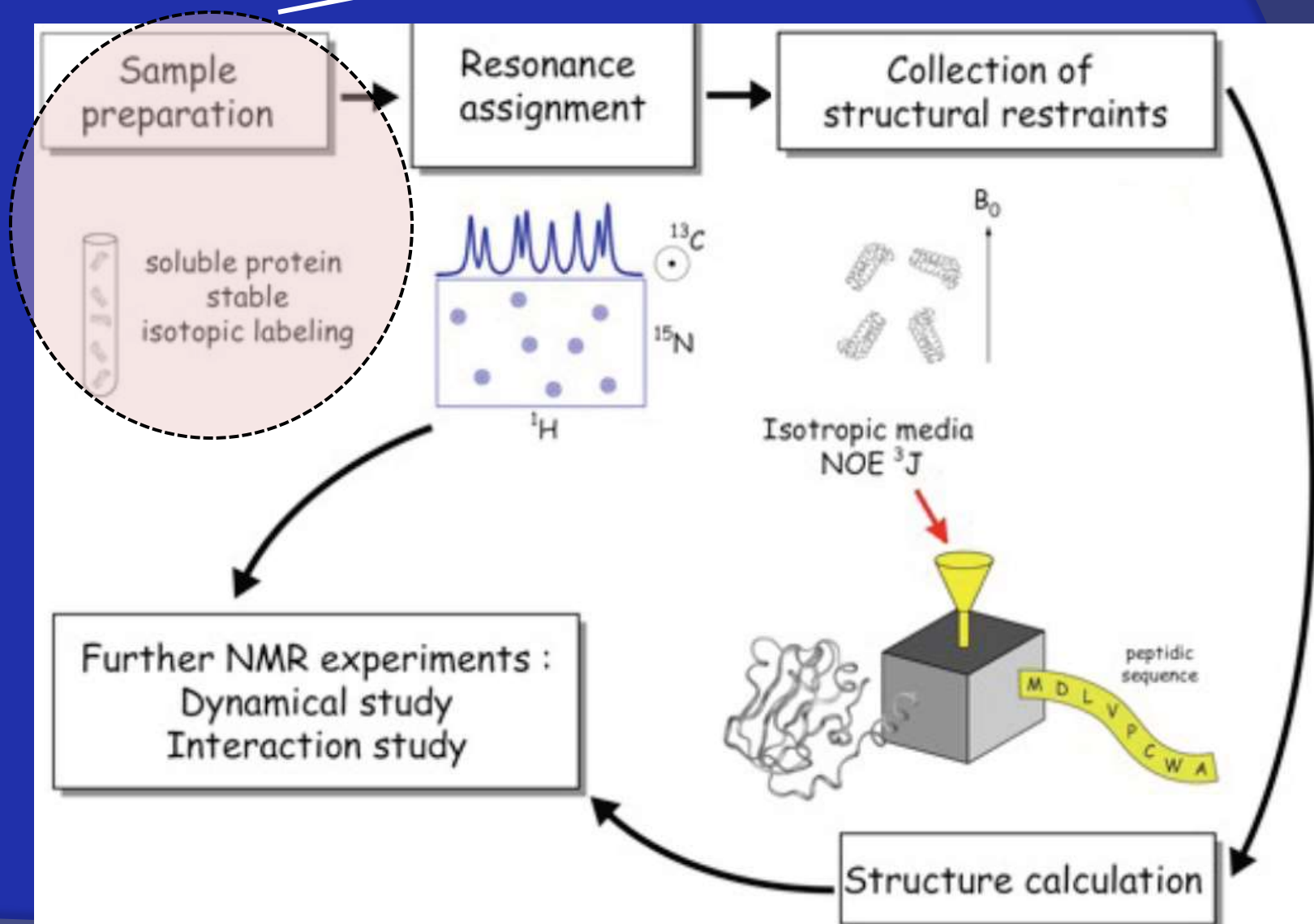
Correctly folded



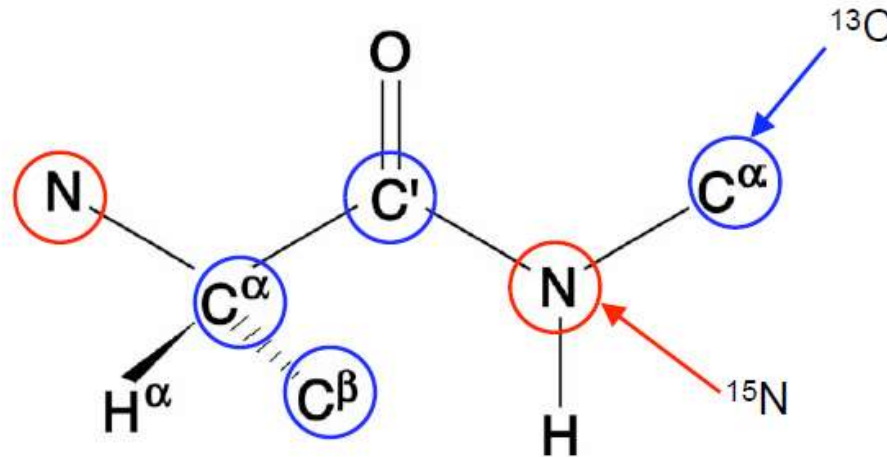
Schematic showing long range nOes in the *lac* headpiece protein

# 蛋白质核磁共振流程

同位素标记



## How to label proteins with stable isotopes?



$^{15}\text{N}$  labeling: use  $^{15}\text{N}$ -labeled ammonium chloride as a source for nitrogen.

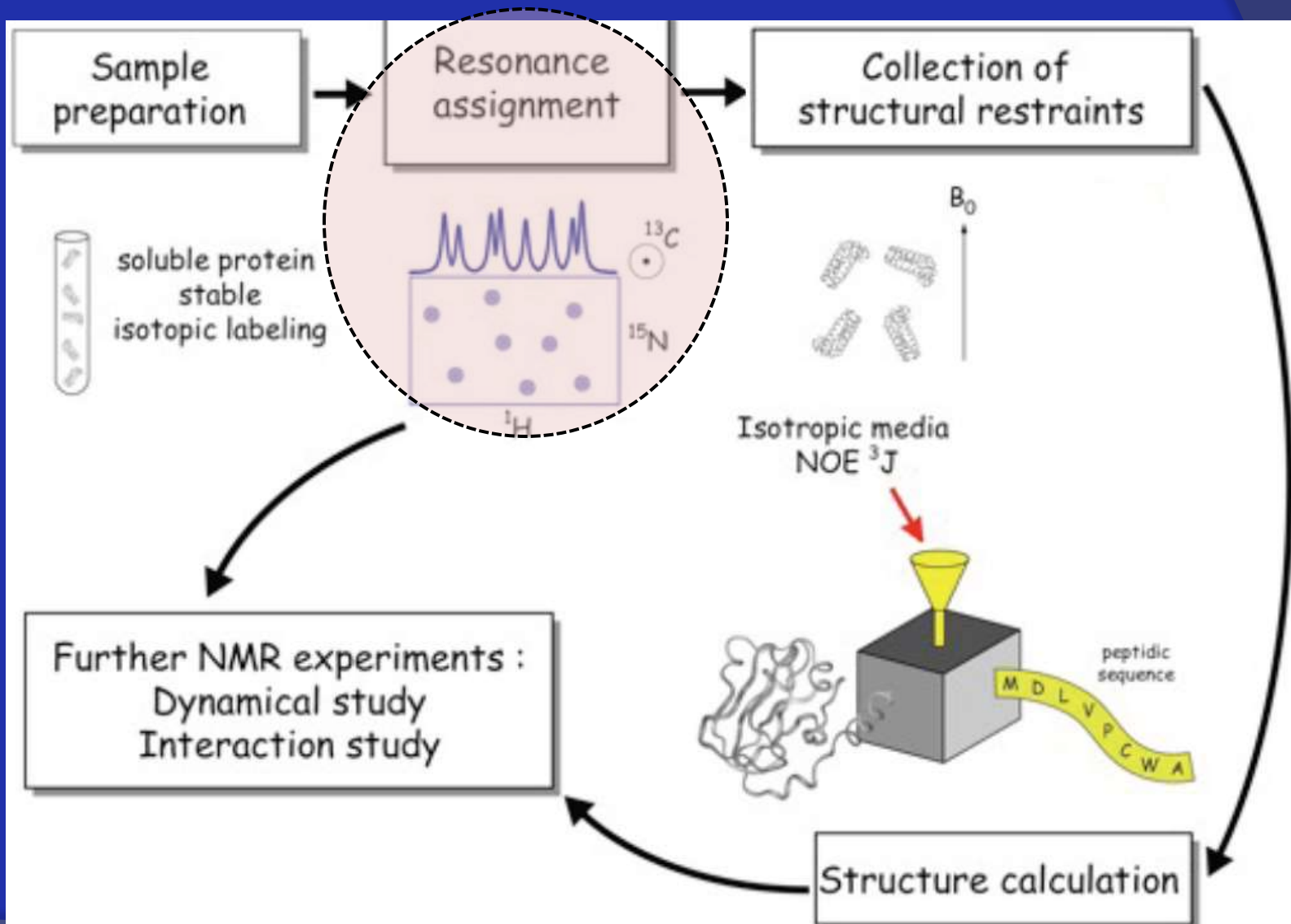
$^{13}\text{C}$  labeling: use  $^{13}\text{C}$ -labeled glucose as a source for carbon.

$^2\text{H}$  labeling: replace  $\text{H}_2\text{O}$  with  $\text{D}_2\text{O}$ .

Selective amino acid labeling: use cells that cannot make the amino acids you want to label and feed the cells with  $^{15}\text{N}$  /  $^{13}\text{C}$ -labeled amino acids.

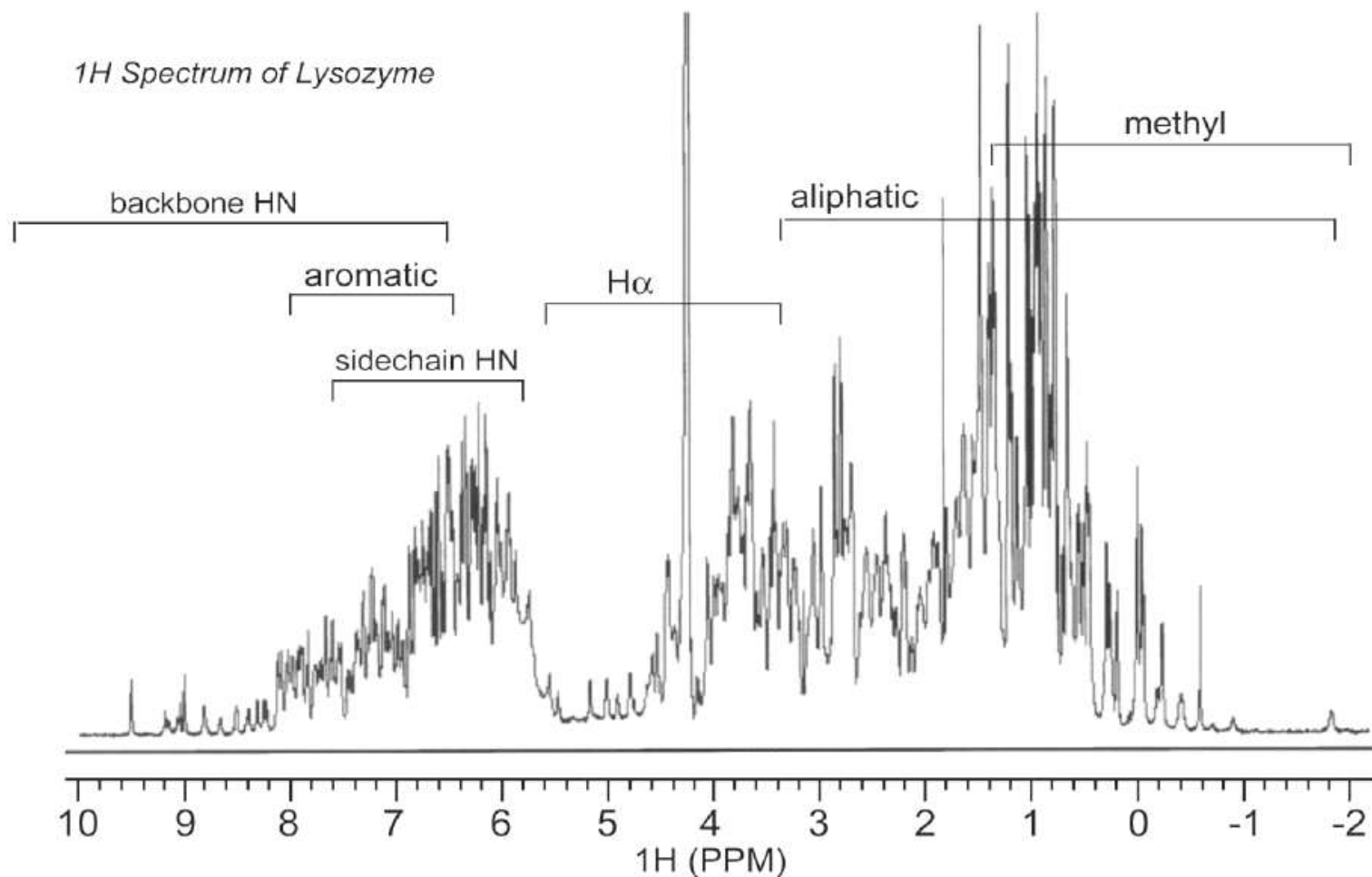
# 蛋白质核磁共振流程

骨架信号归属  
支链信号归属

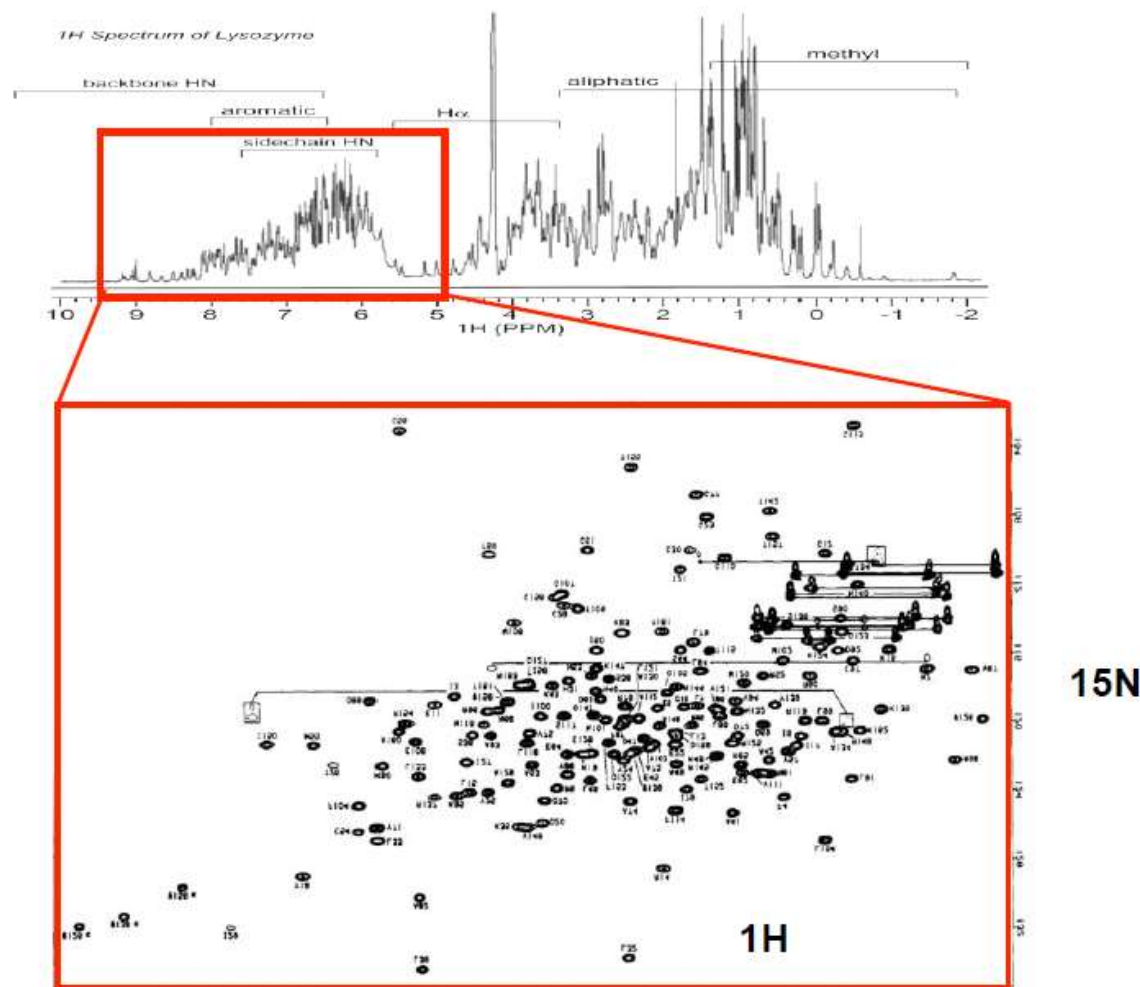


# 蛋白质核磁共振信号归属的基本步骤

1D  $^1\text{H}$  spectrum of lysozyme, at pH 7.0, 25  $^{\circ}\text{C}$ , from 600 MHz magnet

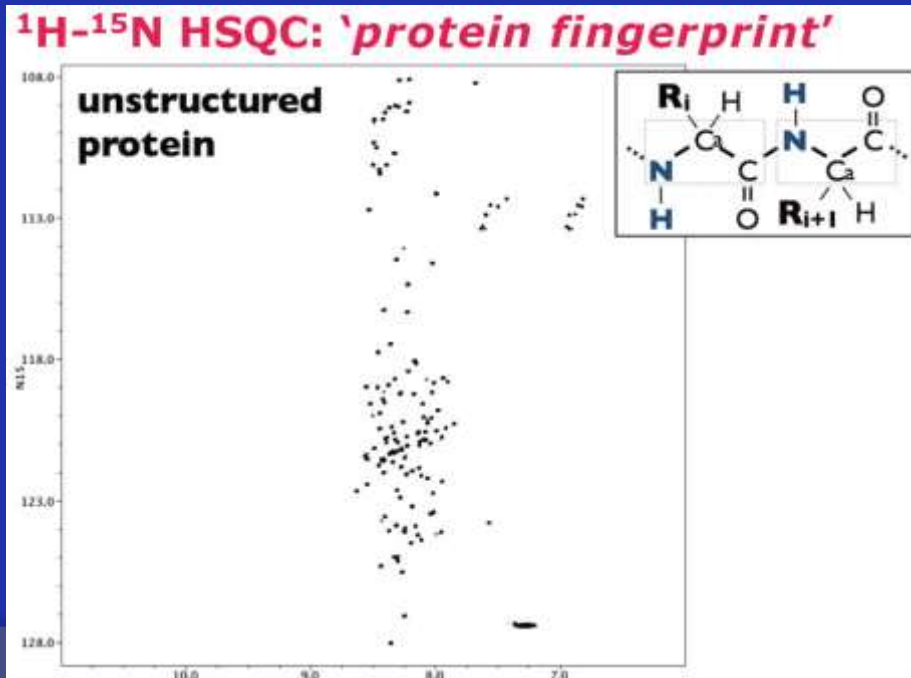
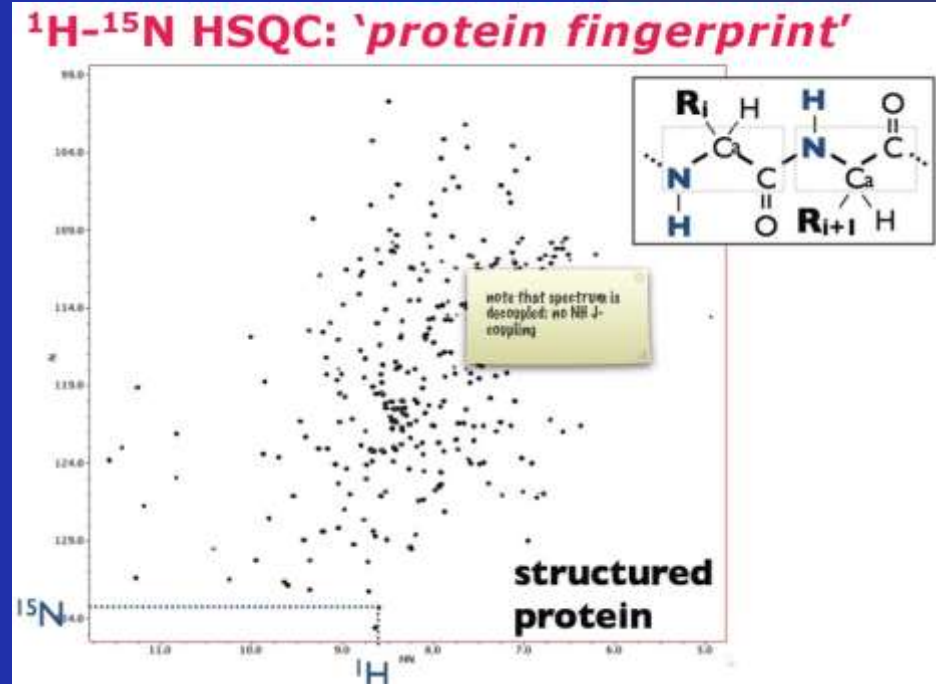


## 2D $^1\text{H}$ - $^{15}\text{N}$ correlation spectrum of lysozyme (HSQC)





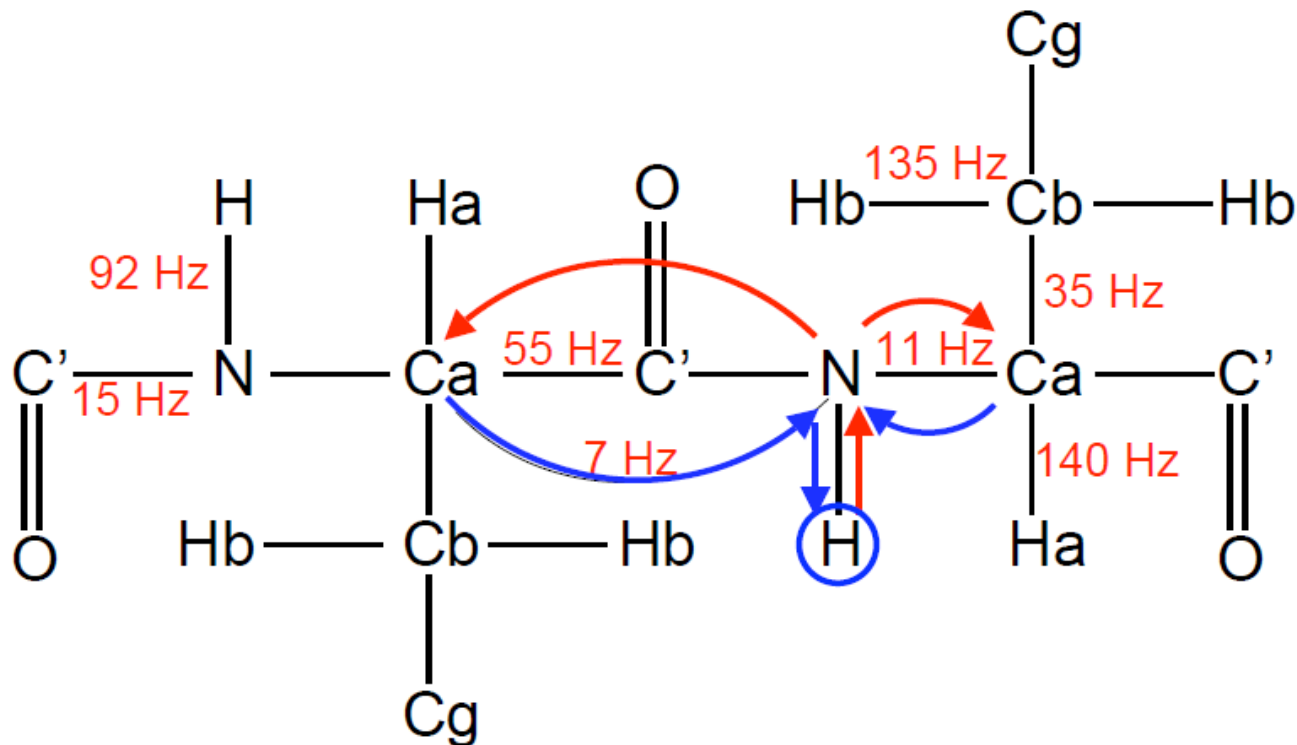
## 蛋白指纹区



有结构蛋白和无结构蛋白的差异

# 蛋白质骨架核磁共振信号归属示例

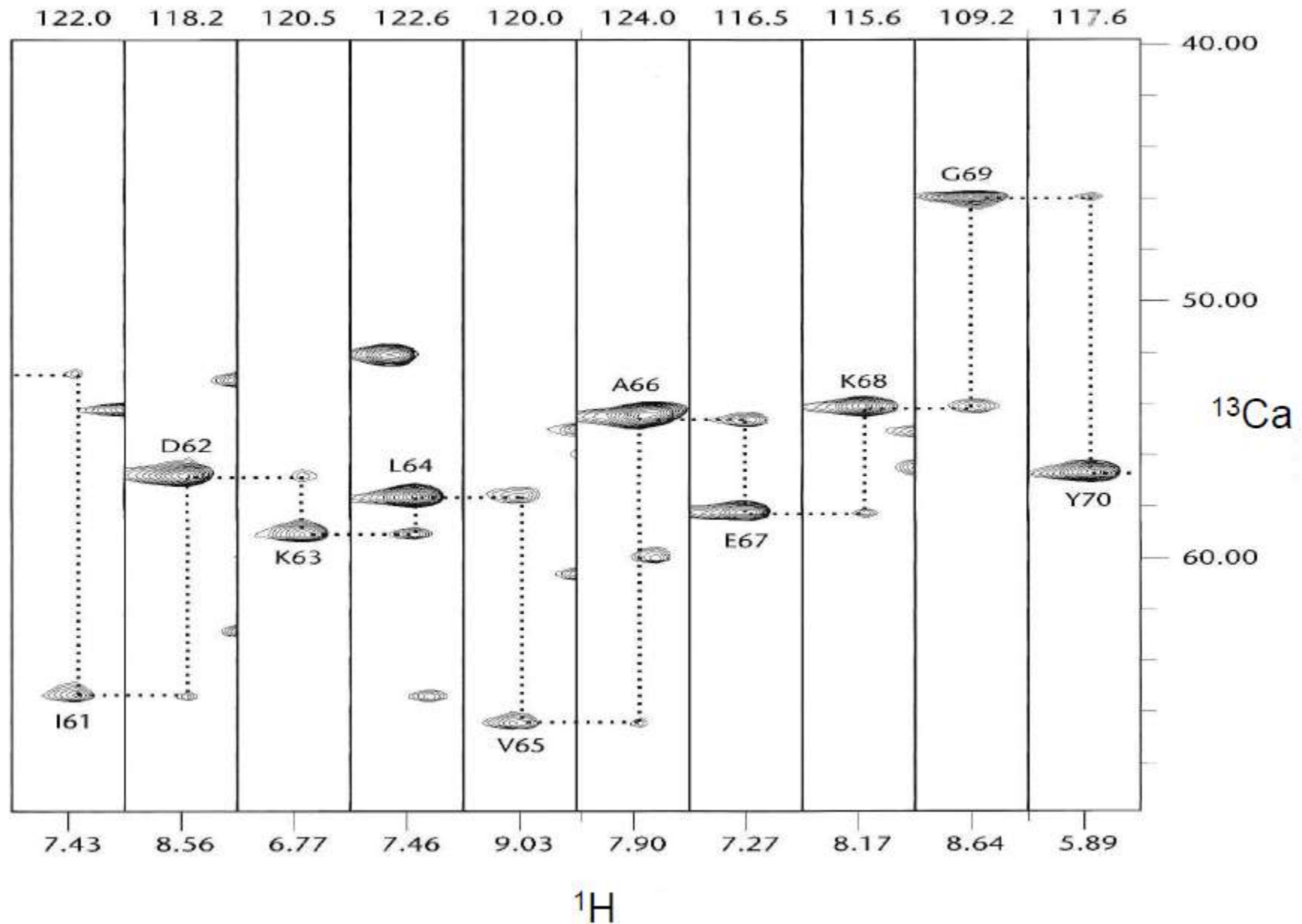
HNCA - correlate  $C^\alpha$  resonances of  $i$  and  $i-1$  residues



$H \rightarrow N \rightarrow C_i^\alpha / C_{i-1}^\alpha \rightarrow (C_i^\alpha / C_{i-1}^\alpha \text{ evolution } t_1) \rightarrow N \rightarrow (N \text{ evolution } t_2) \rightarrow H \rightarrow (H \text{ evolution } t_3)$

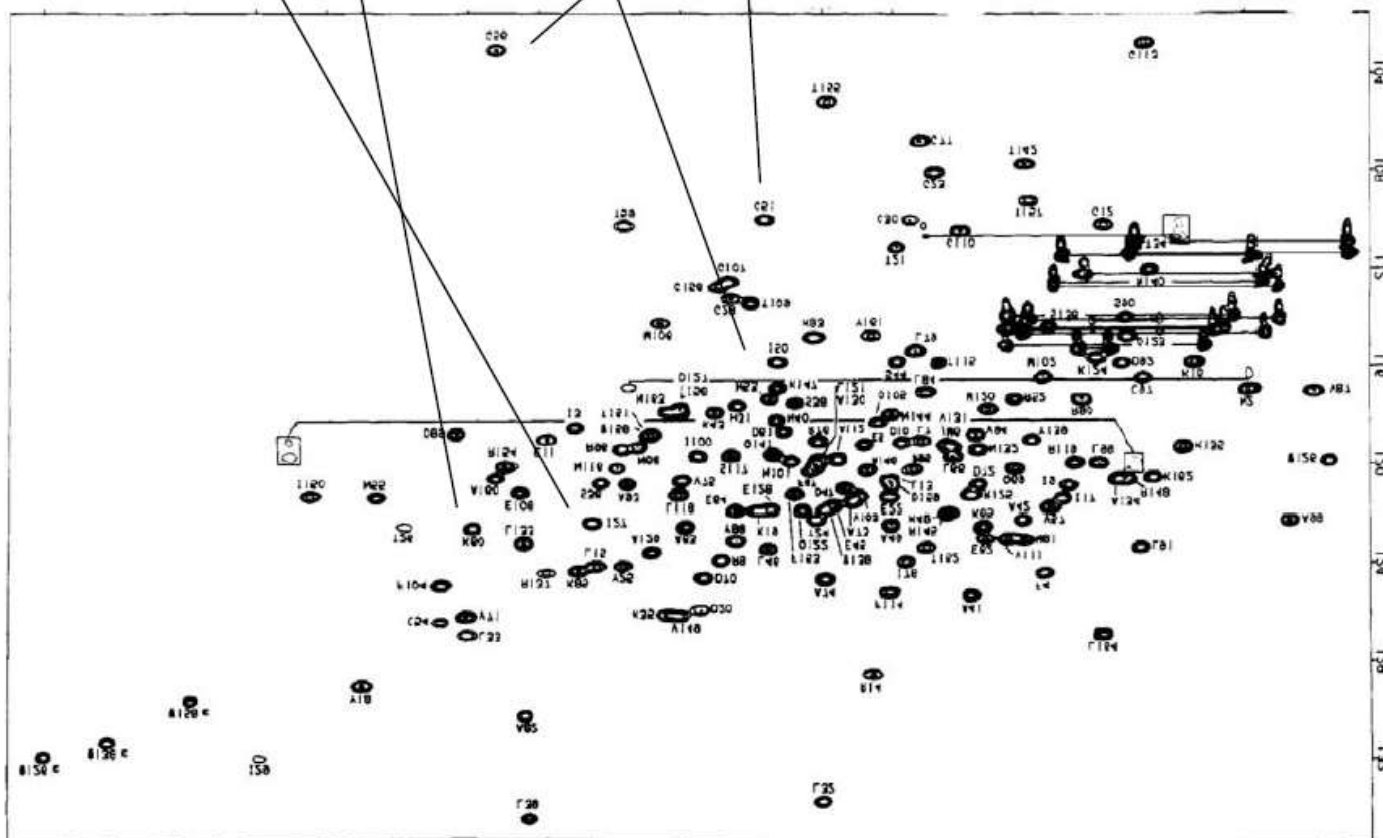


# HN strips from a 3D HNCA Spectrum



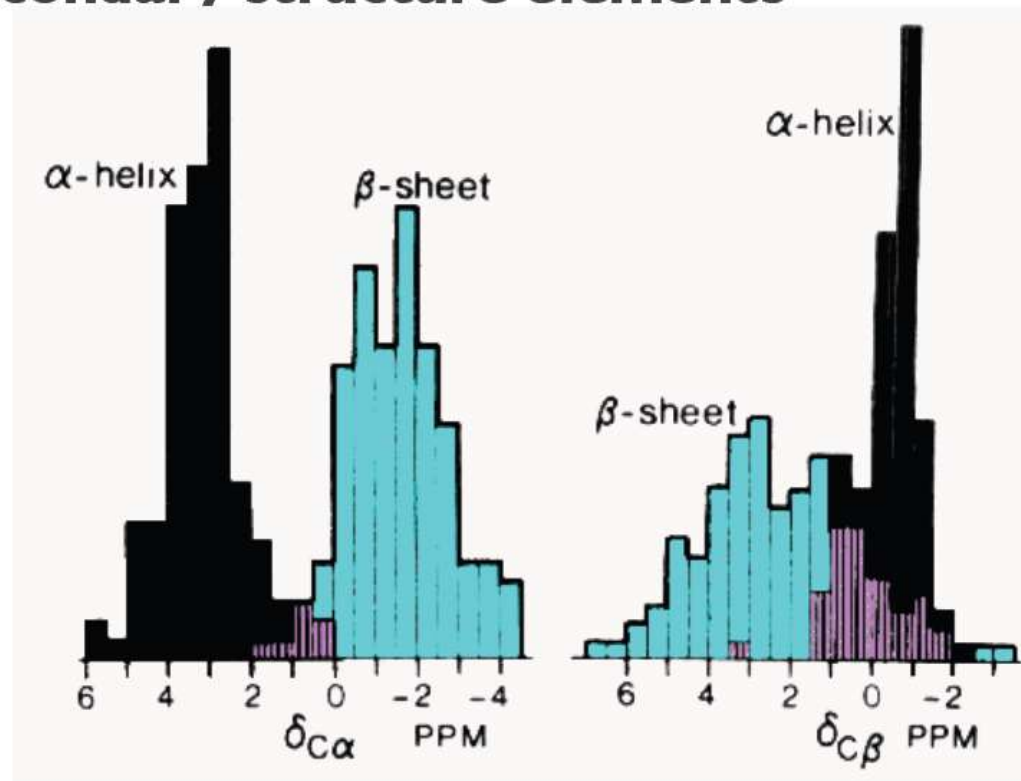
# Sequence specific assignments of NMR resonances

GLKVTSEVALLKREDNNAAGPT ...



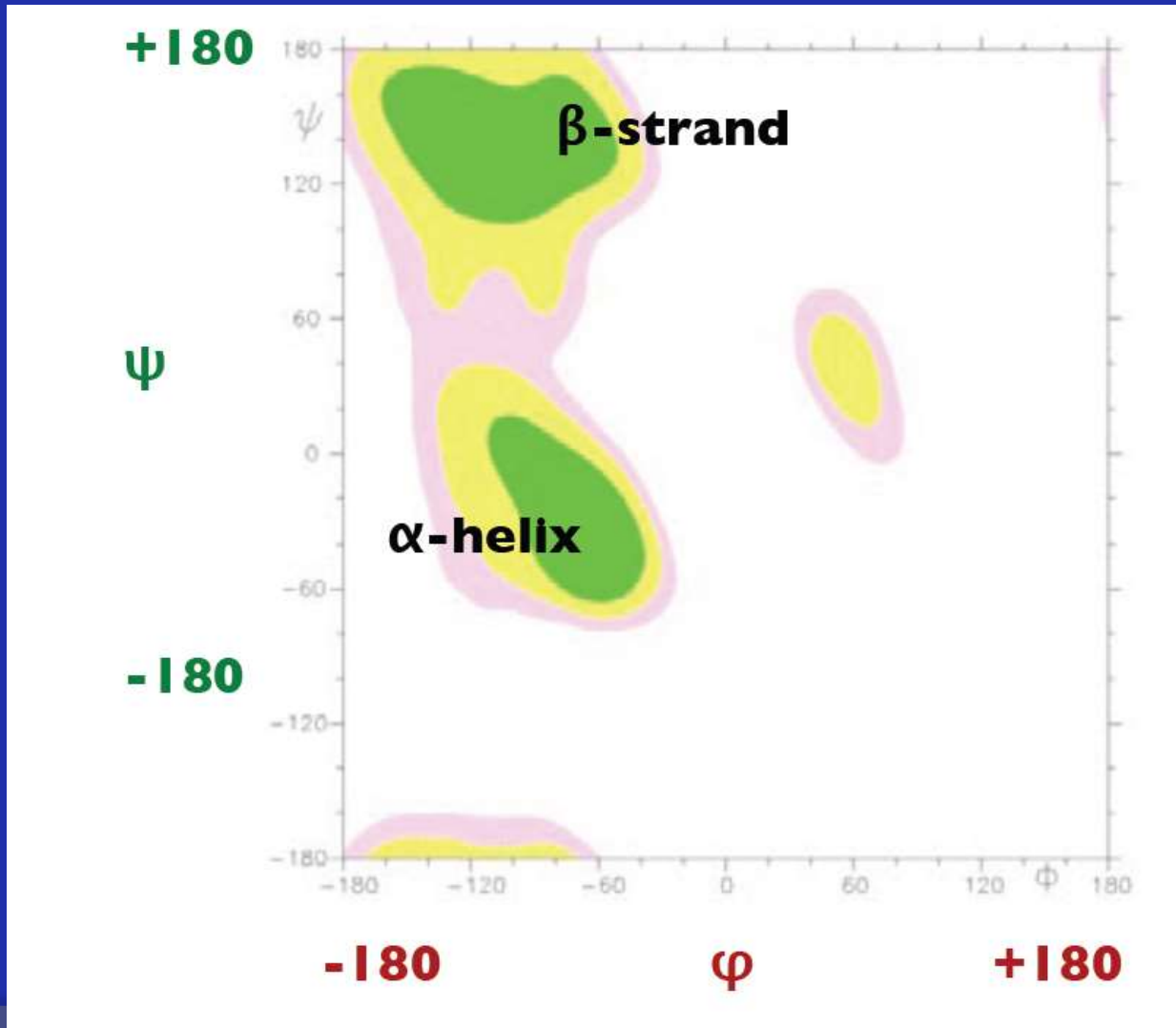
# 化学位移与二面角的关系

- $^{13}\text{C}_\alpha$  and  $^{13}\text{C}_\beta$  chemical shifts
  - sensitive to dihedral angles
  - report on secondary structure elements

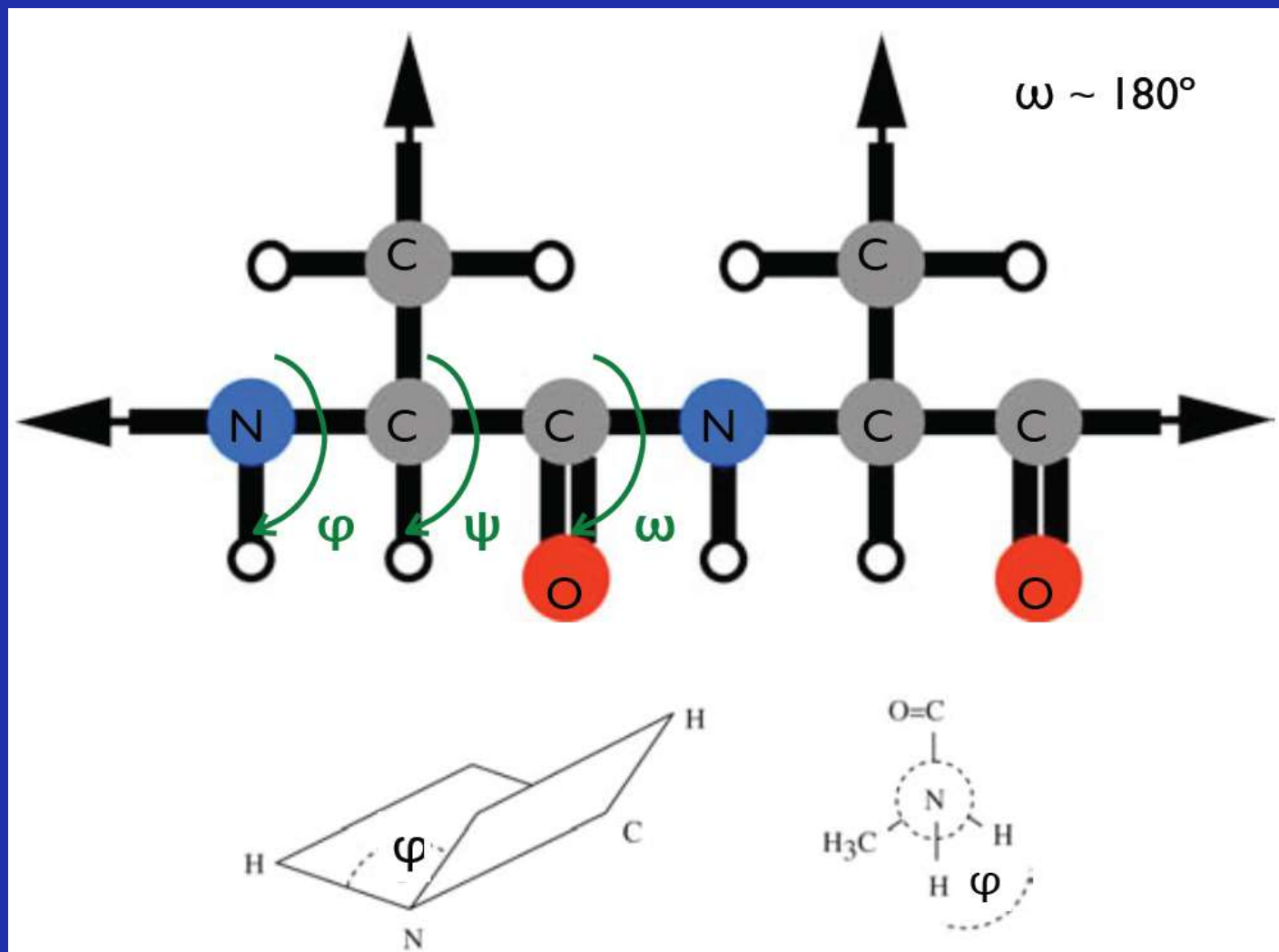


# Dihedral angle restraint

Ramachandran plot

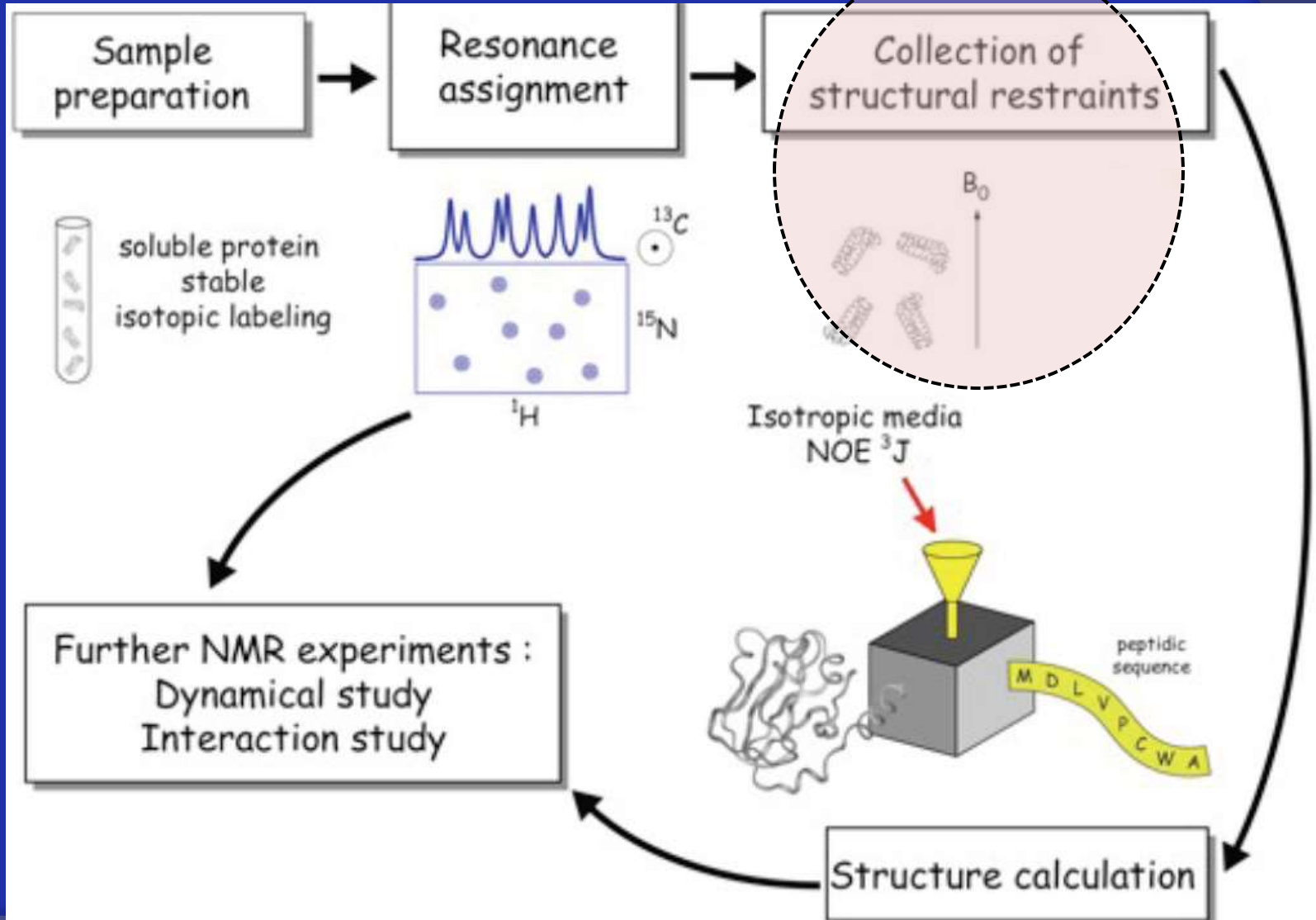


# 二面角定义



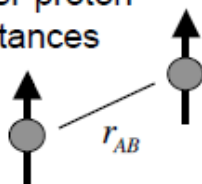
NOEs和J耦合常数

## 蛋白质核磁共振流程

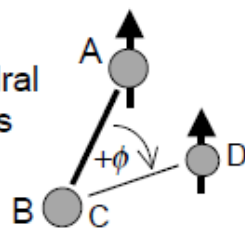


## Measuring structural restraints

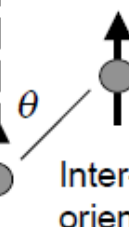
Inter-proton  
distances



Dihedral  
angles



B

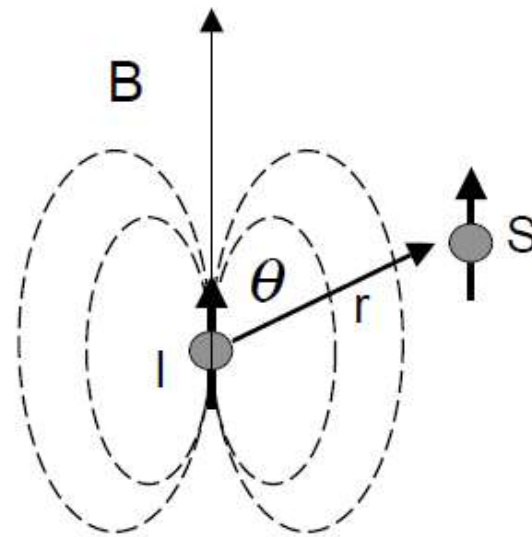
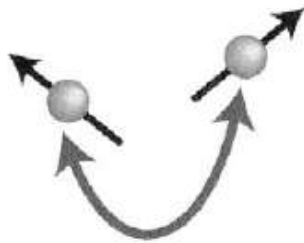


Inter-nuclear vector  
orientations



## Interaction between two magnetic dipole moments

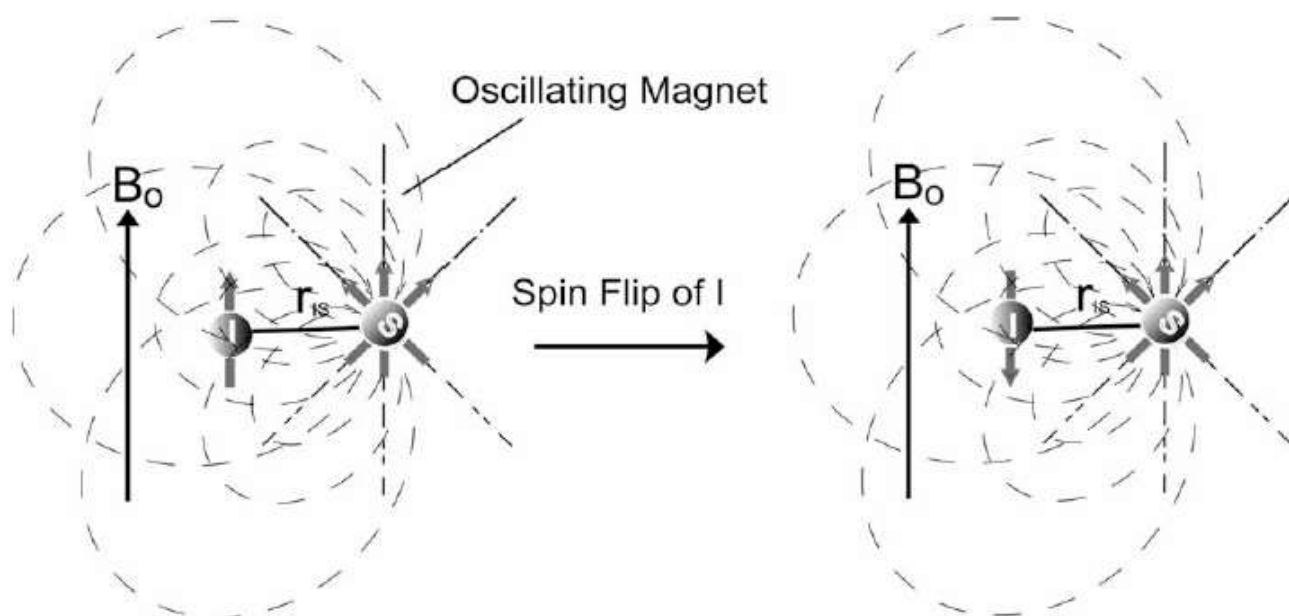
dipolar interaction,  
through-space



$$DC = -\frac{\mu_0 \gamma_I \gamma_S \hbar}{16\pi^3 r^3} (3\cos^2 \theta - 1)$$

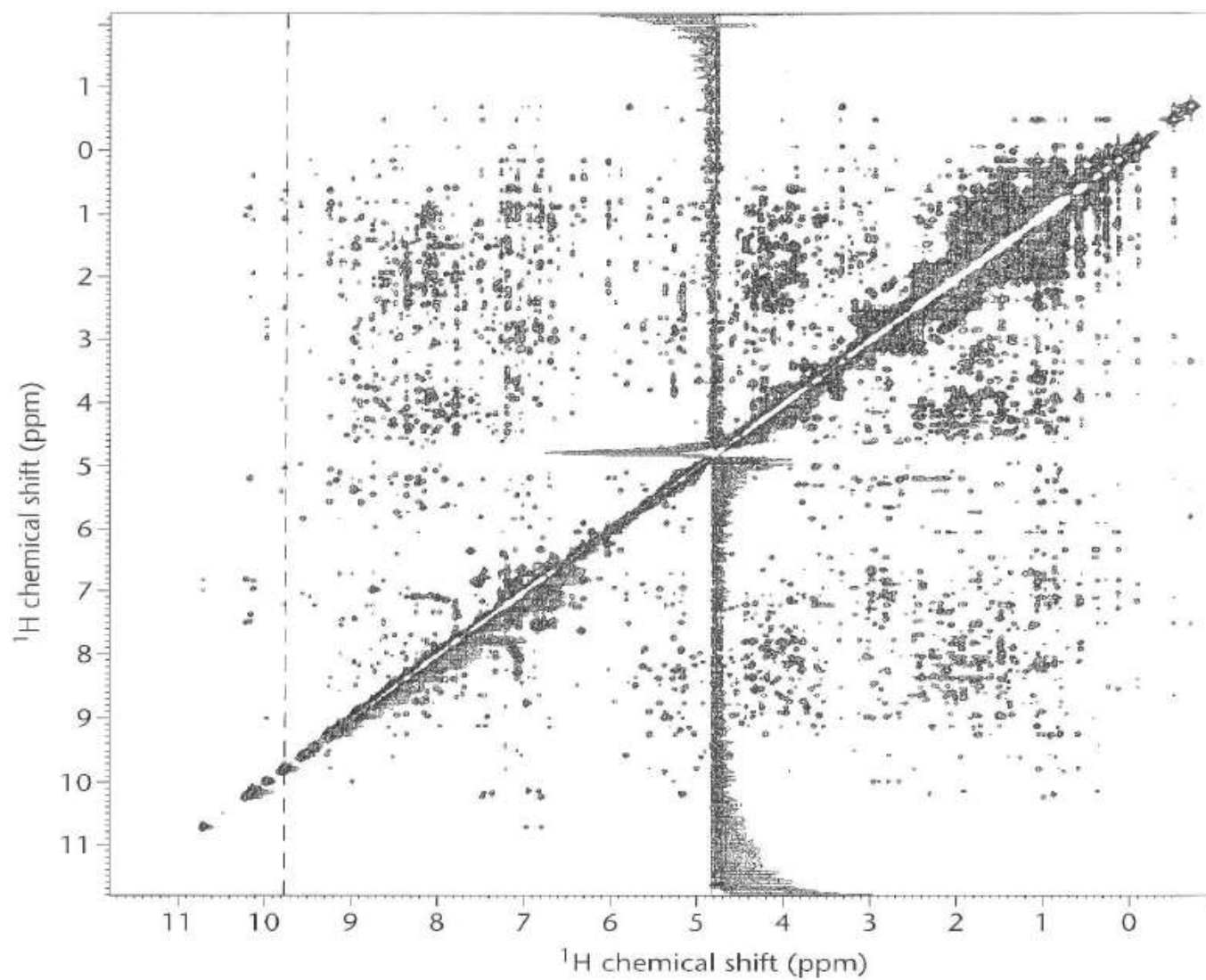
## Nuclear Overhauser Enhancement (NOE) - distance restraints

Because of the dipole-dipole interaction and molecular tumbling, two dipolar-coupled spins in a molecule do not relax independently. The cross-relaxation between them lead to observation of NOE, or transfer of magnetization from one spin to another.



NOE measures  $^1\text{H}$ - $^1\text{H}$  distances and is proportional to  $1/r^6$ . Hence NOE is usually observed when  $r < 5 \text{ \AA}$ . NOE-derived distance restraints are essential for protein structure determination.

2D  $^1\text{H}$ - $^1\text{H}$  NOESY of dioxygenase (179 AA) at pH 7.0, 25  $^{\circ}\text{C}$



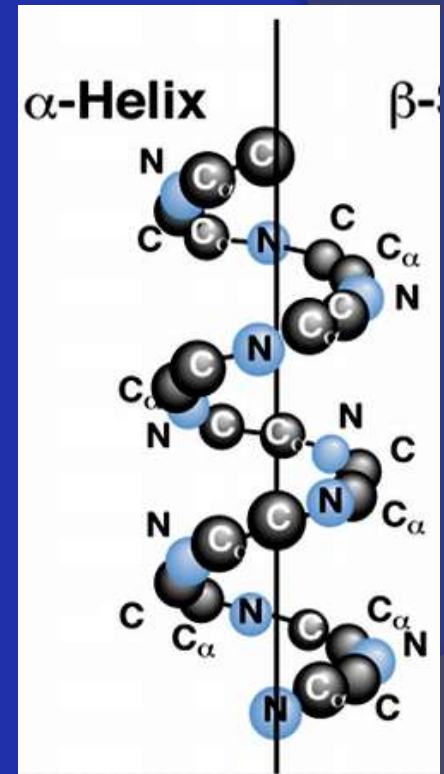
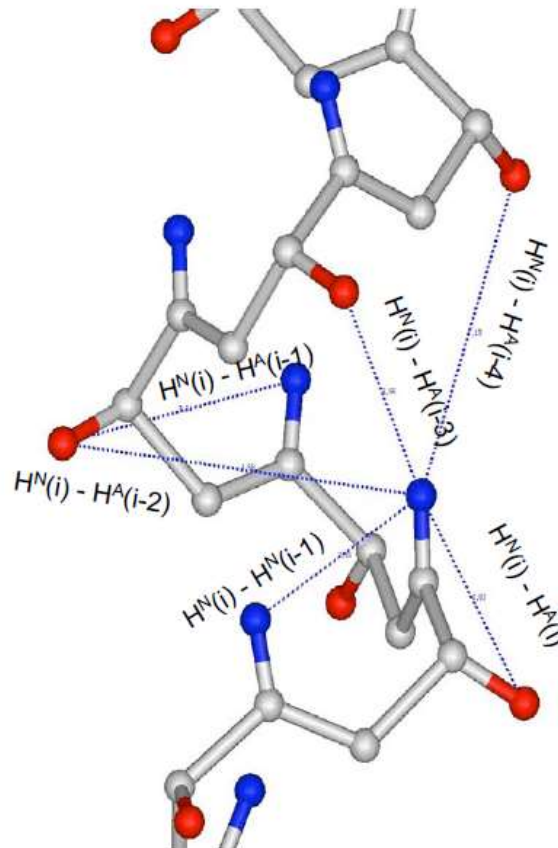
## Characteristic NOEs for helical structures

### $\alpha$ -helix

HN(i) – HN(i+1)	2.8	Å
Ha(i) – HN(i+1)	3.5	Å
Ha(i) – HN(i+2)	4.4	Å
Ha(i) – HN(i+3)	3.4	Å

### $3_{10}$ -helix

HN(i) – HN(i+1)	2.6	Å
Ha(i) – HN(i+1)	3.4	Å
Ha(i) – HN(i+2)	3.8	Å
Ha(i) – HN(i+3)	3.3	Å



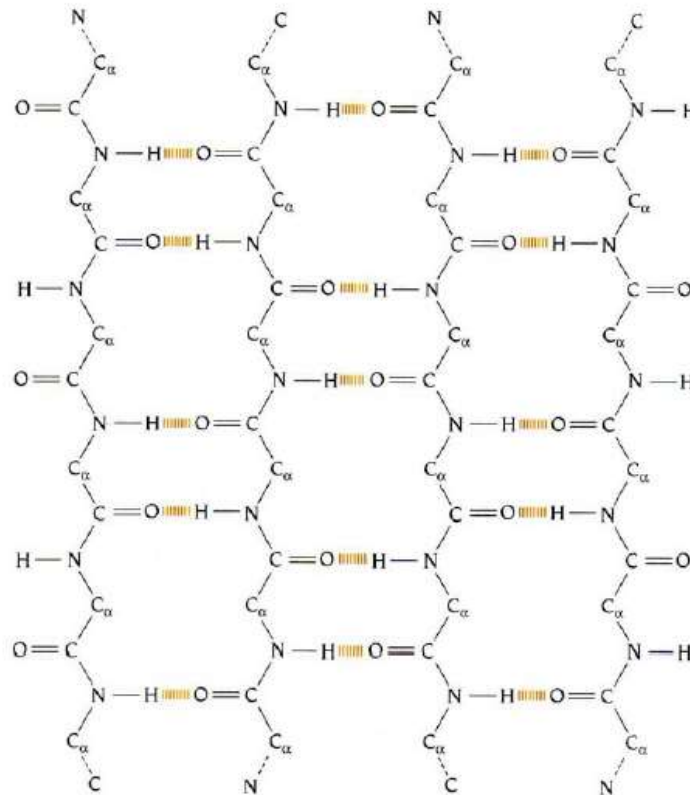
## Characteristic NOEs for $\beta$ structures

### antiparallel $\beta$ -sheet

Ha(i) – HN(i+1)	2.2	Å
Ha(i) – Ha(j)	2.3	Å
Ha(i) – HN(j)	3.2	Å
HN(i) – HN(j)	3.3	Å

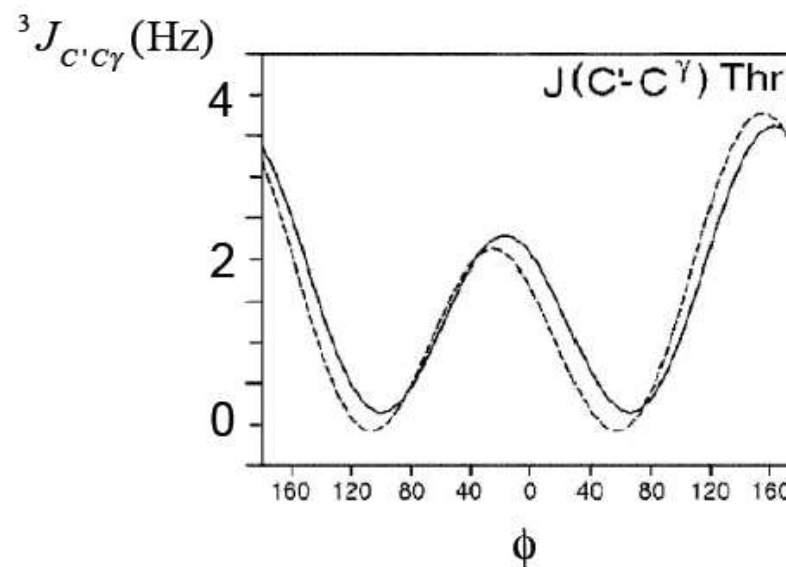
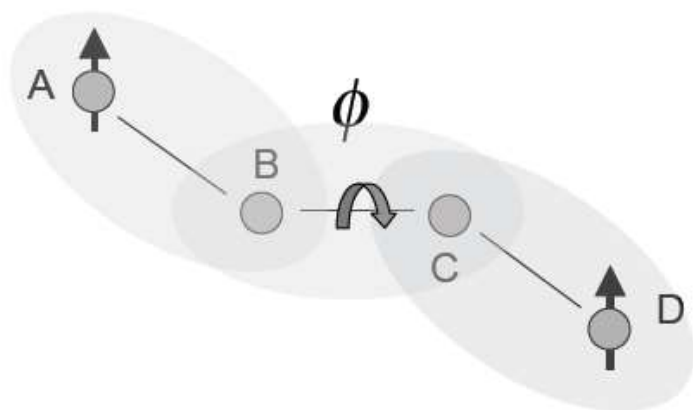
### parallel $\beta$ -sheet

Ha(i) – HN(i+1)	2.2	Å
Ha(i) – Ha(j)	4.8	Å
Ha(i) – HN(j)	3.0	Å
HN(i) – HN(j)	4.0	Å





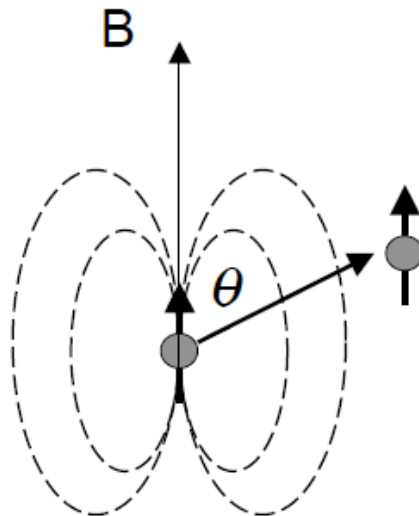
## 3-bond $J$ couplings - dihedral angle restraints



$$^3J = A \cos^2(\phi) + B \cos(\phi) + C$$

Karplus equation

## Dipolar couplings - orientation restraints



$$DC \propto 3\cos^2 \theta - 1$$

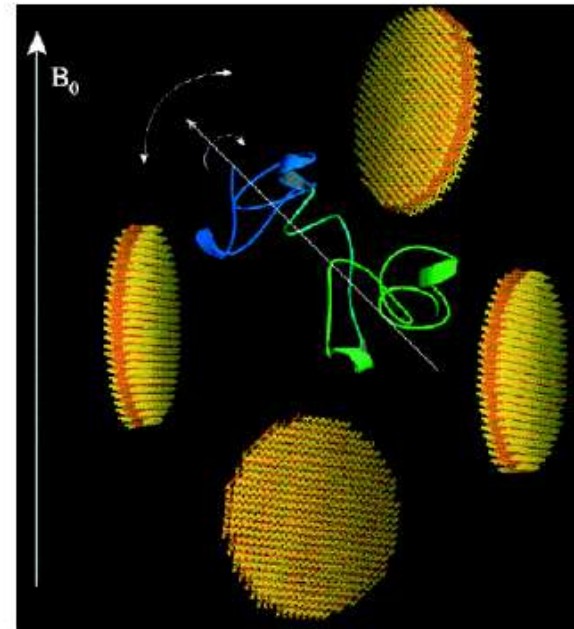
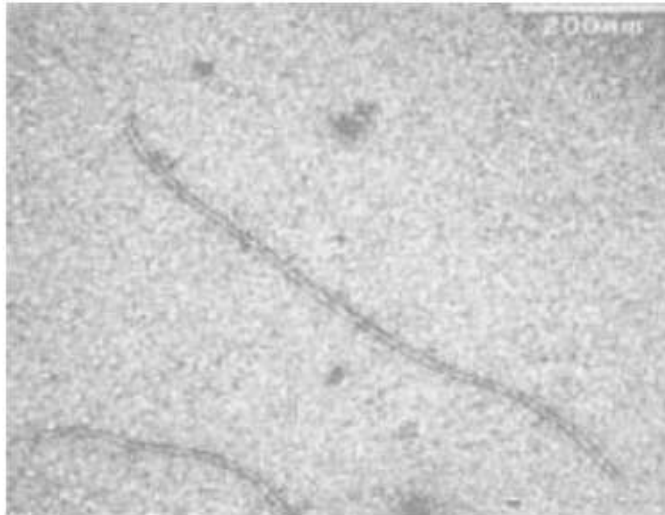
In solution, proteins tumble isotropically. DC from all orientations sum up to zero in the timescale NMR signals are observed.

To measure DC, proteins need to have, on average, a preferred orientation. When proteins are weakly aligned relative to the B field, residual dipolar couplings (RDCs) can be measured.



## Various liquid crystals for marginally orientating proteins

*filamentous phage* (Pf1)

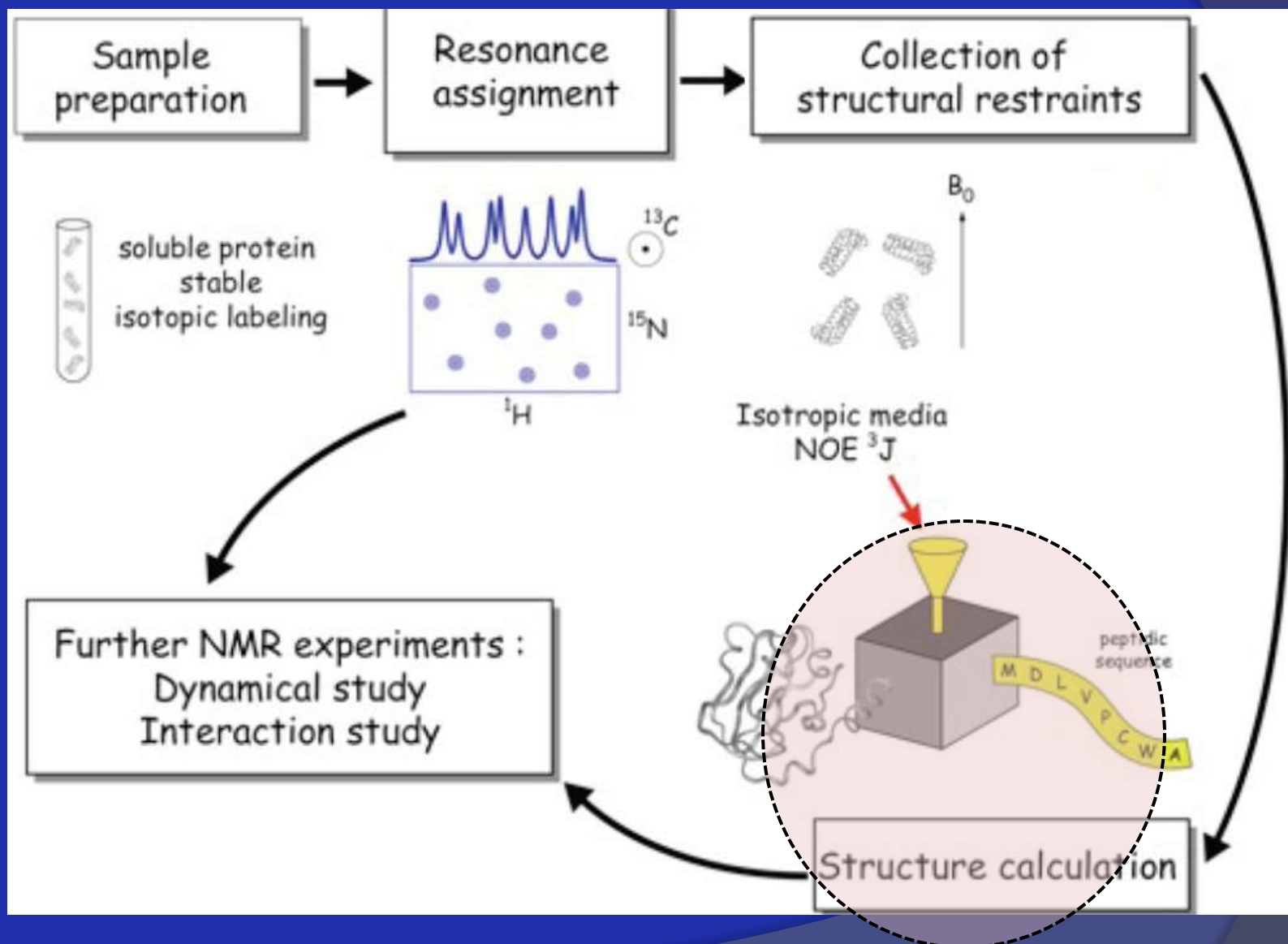


DMPC:DHPC Bicelles

Polyethylene Glycol, hexanol

Cellulose Crystallites, DNA nanotubes

# 蛋白质核磁共振流程



结构计算

## Calculate structures using NMR-derived restraints

Goal: find a structural solution which satisfies all experimental restraints

### Restrained Molecular Dynamics

Basic idea is to solve Newton's equations of motion

$$-\nabla_{q_i} \mathbf{V} = m_i \frac{d^2 r_i}{dt^2},$$

$r_i$  – position of the  $i$ th atom

$m_i$  – mass of the  $i$ th atom

$V$  – total potential energy of the system

**What is  $V$ ?**

## Defining the NMR refinement potential

Total potential  $V$  includes both physical and pseudo potential energies

Physical potentials:

- chemical bonds
- angles
- VDW

Pseudo potentials from experimental restraints:

NOE distance restraints (including HB restraints)

Example: 
$$U_{NOE} = c(r_{ij} - r_{ij}^0)^2$$
$$c \text{ is force constant (kcal mol}^{-1} \text{ \AA}^{-2})$$

Dihedral restraints:  $\phi$ ,  $\psi$ ,  $\chi_1$ , and  $\chi_2$

Dipolar coupling restraints – vector orientation

## The simulated annealing structure calculation protocol

### *Why use simulated annealing?*

Due to the complexity of the potential and thus the energy landscape, MD often gets stuck in false local minima.

### *Protocol*

increase the momentum of all particles in a MD run by raising the temperature or increasing the mass of particles

lower all other potentials except for the NMR potentials; this is to get around the local minima by satisfying the NMR restraints

annealing: slowly reduce temperature (mass) and increase the VDW force constants to reach the global minimum

## An example of SA/MD calculation protocol in XPLOR-NIH

$T(\text{initial}) = 2000 \text{ K}$        $T(\text{final}) = 200 \text{ K}$

Compute energy

While  $T > T(\text{final})$

$T = T - dT$

Compute energy

Increase the force constant of NMR restraint potential

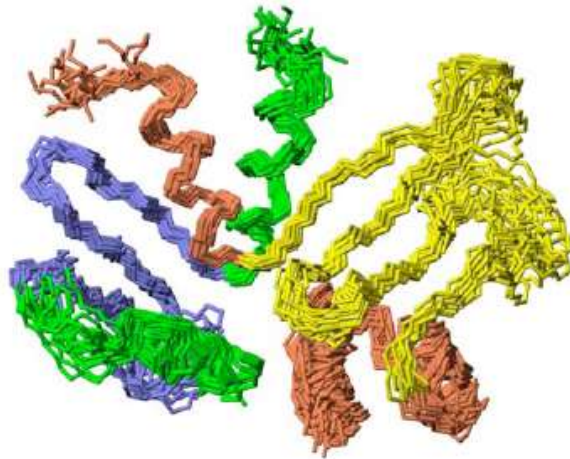
Increase VDW

Verlet dynamics at  $T$  for  $\sim 10 \text{ ps}$

End Cooling Loop

Final Powell energy minimization

**Calculate many structures starting from the random templates each time**

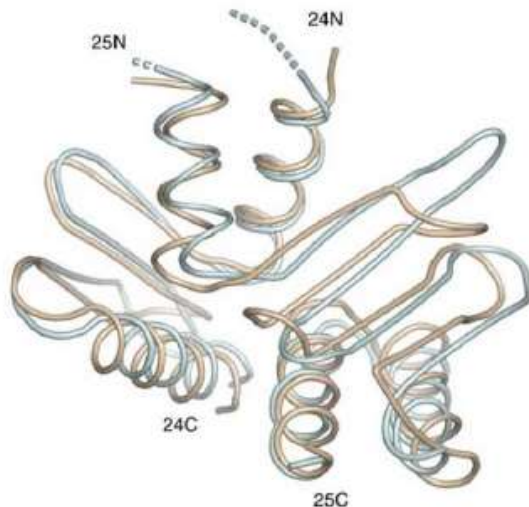


Select an ensemble of 20 structures with lowest energy

Coordinate precision

All heavy atoms 1.55 Å

Backbone heavy atoms 1.05 Å



Comparison between the NMR and X-ray structures



**Table 1 NMR structural statistics and atomic r.m.s. differences<sup>1</sup>**

Quantity	Number of restraints	Vio. per struct.
NOEs	681	0.25 +/- 0.55 (> 0.2 Å)
Intramolecular	165 / 467	
Intermolecular	49	
Dihedral angle restraints	34	0
$\chi^1$	10 / 13	0
$\chi^2$	11 / 0	0
Dipolar coupling restraints (Hz) <sup>2</sup>	173	2.55 +/- 0.12
NH	50 / 62	2.05 +/- 0.11
C'C $^\alpha$	0 / 61	3.30 +/- 0.19
Other restraints		
H-bond	26 / 38	0.45 +/- 0.69 (> 0.1 Å)
$\phi/\psi$	58 / 115	0.2 +/- 0.41 (> 2.5°)

<sup>1</sup>Statistics are calculated and averaged over the 20 structures with the lowest overall energy. Numbers are reported for the combined dimer or the individual monomers (spc24 / spc25).

<sup>2</sup>Violations are given as the r.m.s. difference (in Hz) between individual sets of experimental dipolar couplings and those predicted by the 20 final structures by means of SVD fit. The  $^1D_{C'C_\alpha}$  couplings are normalized to  $^1D_{NH}$ .

<sup>3</sup>The precision of the atomic coordinates is defined as the average r.m.s. difference between the 20 final structures and their mean coordinates.